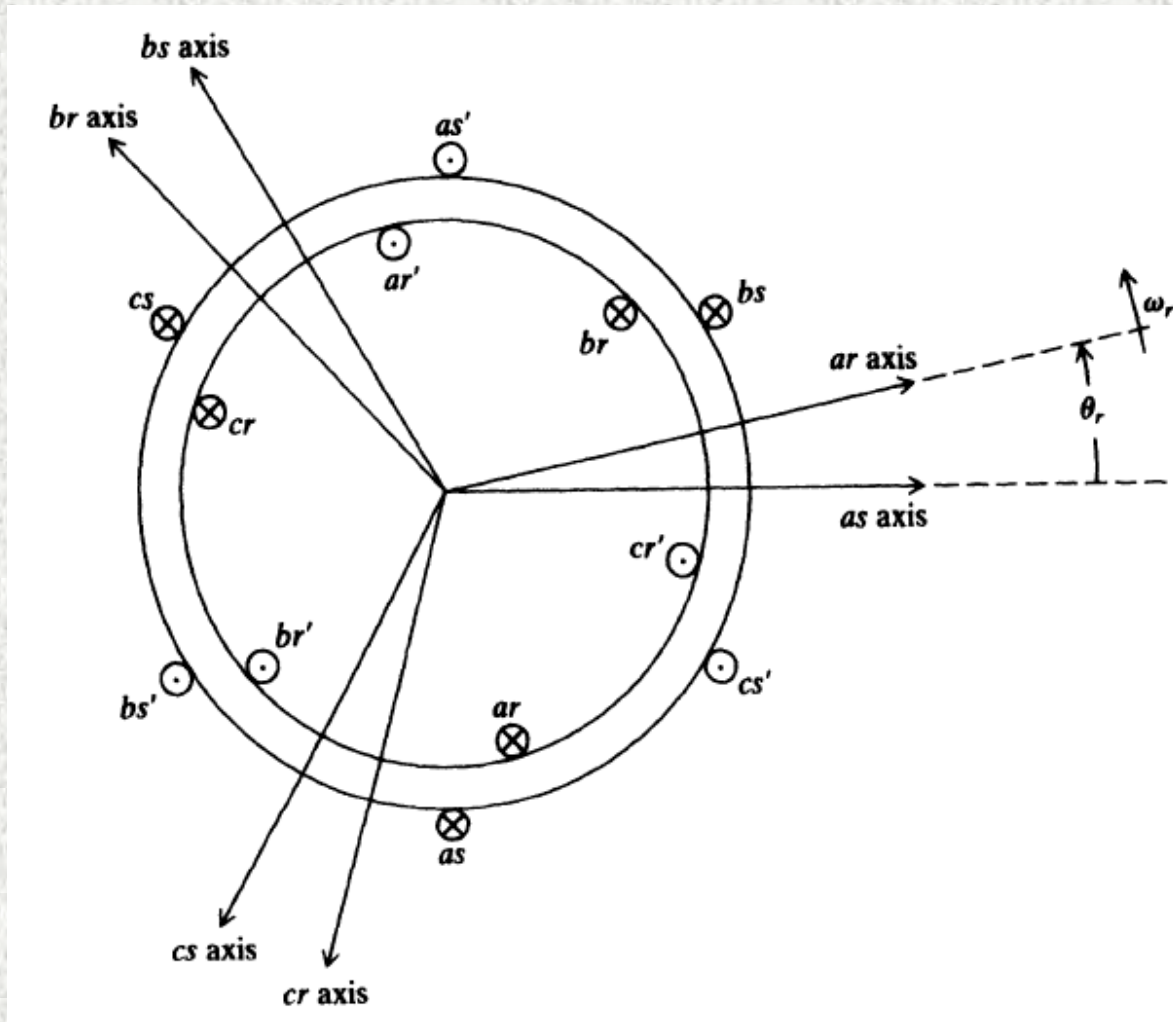
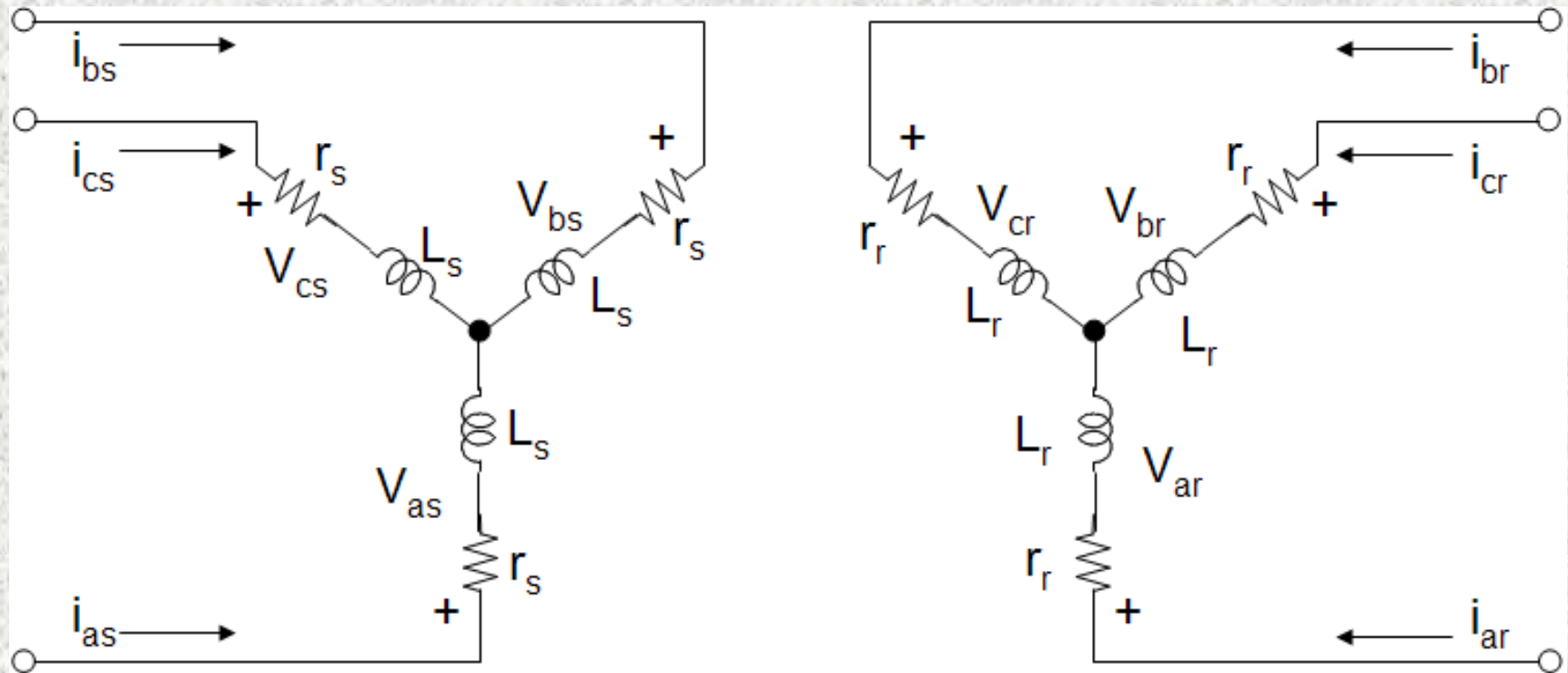


3-Phase Induction Machines



A 2-pole, 3-phase symmetrical induction machine.

3-Phase Induction Machines



A 2-pole, 3-phase symmetrical induction machine.

3-Phase Induction Machines

- In abc reference frame, voltage equations can be written as

$$V_{abcs} = r_s i_{abcs} + p \lambda_{abcs}$$

$$V_{abcr} = r_r i_{abcr} + p \lambda_{abcr}$$

$$(f_{abcs})^T = [f_{as} \quad f_{bs} \quad f_{cs}], \quad (f_{abcr})^T = [f_{ar} \quad f_{br} \quad f_{cr}]$$

s: denotes variables and parameters associated with the stator circuits.

r: denotes variables and parameters associated with the rotor circuits.

3-Phase Induction Machines

$$\begin{bmatrix} \lambda_{abcs} \\ \lambda_{abc r} \end{bmatrix} = \begin{bmatrix} L_s & L_{sr} \\ (L_{sr})^T & L_r \end{bmatrix} \begin{bmatrix} i_{abcs} \\ i_{abc r} \end{bmatrix}$$

where,

$$\mathbf{L}_s = \begin{bmatrix} L_{ls} + L_{ms} & -\frac{1}{2}L_{ms} & -\frac{1}{2}L_{ms} \\ -\frac{1}{2}L_{ms} & L_{ls} + L_{ms} & -\frac{1}{2}L_{ms} \\ -\frac{1}{2}L_{ms} & -\frac{1}{2}L_{ms} & L_{ls} + L_{ms} \end{bmatrix}, \quad \mathbf{L}_r = \begin{bmatrix} L_{lr} + L_{mr} & -\frac{1}{2}L_{mr} & -\frac{1}{2}L_{mr} \\ -\frac{1}{2}L_{mr} & L_{lr} + L_{mr} & -\frac{1}{2}L_{mr} \\ -\frac{1}{2}L_{mr} & -\frac{1}{2}L_{mr} & L_{lr} + L_{mr} \end{bmatrix}$$

L_{ls} and L_{ms} are, respectively, the leakage and magnetizing inductance of the stator windings.

L_{lr} and L_{mr} are, respectively, the leakage and magnetizing inductance of the rotor windings.

3-Phase Induction Machines

$$\mathbf{L}_{sr} = \mathbf{L}_{rs} = L_{rs} \begin{bmatrix} \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) \\ \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) \\ \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r \end{bmatrix},$$

L_{sr} : the mutual inductances between stator and rotor windings

- squirrel-cage rotor: the current flows in copper or aluminum bars which are uniformly distributed in a common ring at each end of the rotor
- in a practical machine, the rotor conductors are skewed slightly with the axis of rotation to reduce the magnitude of harmonic torques

Referring all rotor variables to the stator windings

- Rotor variables can be referred to the stator windings by appropriate turns ratio:

$$i'_{abc} = \frac{N_r}{N_s} i_{abc}, \quad V'_{abc} = \frac{N_s}{N_r} V_{abc}, \quad \lambda'_{abc} = \frac{N_s}{N_r} \lambda_{abc}, \quad L_{ms} = \left(\frac{N_s}{N_r} \right)^2 L_{sr}$$

$$[\mathbf{L}'_{sr}] = \frac{N_s}{N_r} [\mathbf{L}_{sr}] = L_{ms} \begin{bmatrix} \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) \\ \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) \\ \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r \end{bmatrix},$$

Referring all rotor variables to the stator windings

■ Also,

$$L_{mr} = \left(\frac{N_r}{N_s} \right)^2 L_{ms}, \quad [\mathbf{L}'_r] = \left(\frac{N_r}{N_s} \right)^2 [\mathbf{L}_r]$$

$$[\mathbf{L}'_r] = \begin{bmatrix} L'_{lr} + L_{mr} & -\frac{1}{2} L_{ms} & -\frac{1}{2} L_{ms} \\ -\frac{1}{2} L_{ms} & L_{lr} + L_{ms} & -\frac{1}{2} L_{ms} \\ -\frac{1}{2} L_{ms} & -\frac{1}{2} L_{ms} & L_{lr} + L_{ms} \end{bmatrix}$$

where,

$$L'_{lr} = \left(\frac{N_s}{N_r} \right)^2 L_{lr}$$

Referring all rotor variables to the stator windings

- Flux linkage may be expressed as

$$\begin{bmatrix} \lambda_{abcs} \\ \lambda'_{abcr} \end{bmatrix} = \begin{bmatrix} \mathbf{L}_s & \mathbf{L}'_{sr} \\ (\mathbf{L}'_{sr})^T & \mathbf{L}'_r \end{bmatrix} \begin{bmatrix} i_{abcs} \\ i'_{abcr} \end{bmatrix}$$

- Voltage equations expressed in terms of machine variables referred to the stator windings may be written as

$$\begin{bmatrix} V_{abcs} \\ V'_{abcr} \end{bmatrix} = \begin{bmatrix} \mathbf{r}_s + p\mathbf{L}_s & p\mathbf{L}'_{sr} \\ p(\mathbf{L}'_{sr})^T & \mathbf{r}'_r + p\mathbf{L}'_r \end{bmatrix} \begin{bmatrix} i_{abcs} \\ i'_{abcr} \end{bmatrix}$$

where,

$$r'_r = \left(\frac{N_s}{N_r} \right)^2 r_r$$

Torque Equation in Machine Variables

- Energy stored in the coupling field may be written as:

$$W_c = W_f = \frac{1}{2} (i_{abcs})^T (\mathbf{L}_s - \mathbf{L}_{ls} \mathbf{I}) i_{abcs} + (i_{abcs})^T (\mathbf{L}_{sr}) i'_{abcr} + \frac{1}{2} (i'_{abcr})^T (\mathbf{L}'_r - \mathbf{L}'_{lr} \mathbf{I}) i'_{abcr}$$

where, \mathbf{I} : identity matrix

- Voltage equations expressed in terms of machine variables referred to the stator windings may be written as:

$$T_e(i_j, \theta_r) = \frac{P}{2} \frac{\partial W_c(i_j, \theta_r)}{\partial \theta_r}$$

Torque Equation in Machine Variables

- Since \mathbf{L}_s and \mathbf{L}_r are functions of θ_r , the above equation for the electromagnetic torque yields.

$$T_e = \left(\frac{P}{2}\right) (i_{abc s})^T \frac{\partial}{\partial \theta_r} [\mathbf{L}'_{sr}] i'_{abc r}$$

$$= -\frac{P}{2} L_{ms} \left\{ \begin{aligned} & \left[i_{as} (i'_{ar} - \frac{1}{2} i'_{br} - \frac{1}{2} i'_{cr}) + i_{bs} (i'_{br} - \frac{1}{2} i'_{ar} - \frac{1}{2} i'_{cr}) + i_{cs} (i'_{cr} - \frac{1}{2} i'_{br} - \frac{1}{2} i'_{ar}) \right] \sin \theta_r \\ & + \frac{\sqrt{3}}{2} [i_{as} (i'_{br} - i'_{cr}) + i_{bs} (i'_{cr} - i'_{ar}) + i_{cs} (i'_{ar} - i'_{br})] \cos \theta_r \end{aligned} \right\}$$

- The torque and rotor speed are related by

$$T_e = J \left(\frac{2}{P} \right) p \omega_r + T_L$$

Transformation of Rotor Windings to the Arbitrary Reference Frame

- In the analysis of induction machines it is desirable to transform the variables associated with the symmetrical rotor windings to the arbitrary reference frame.

$$f'_{qd0r} = \mathbf{K}_r f'_{abcr}$$

$$(f'_{qd0r})^T = \begin{bmatrix} f'_{qr} & f'_{dr} & f'_{0r} \end{bmatrix}$$

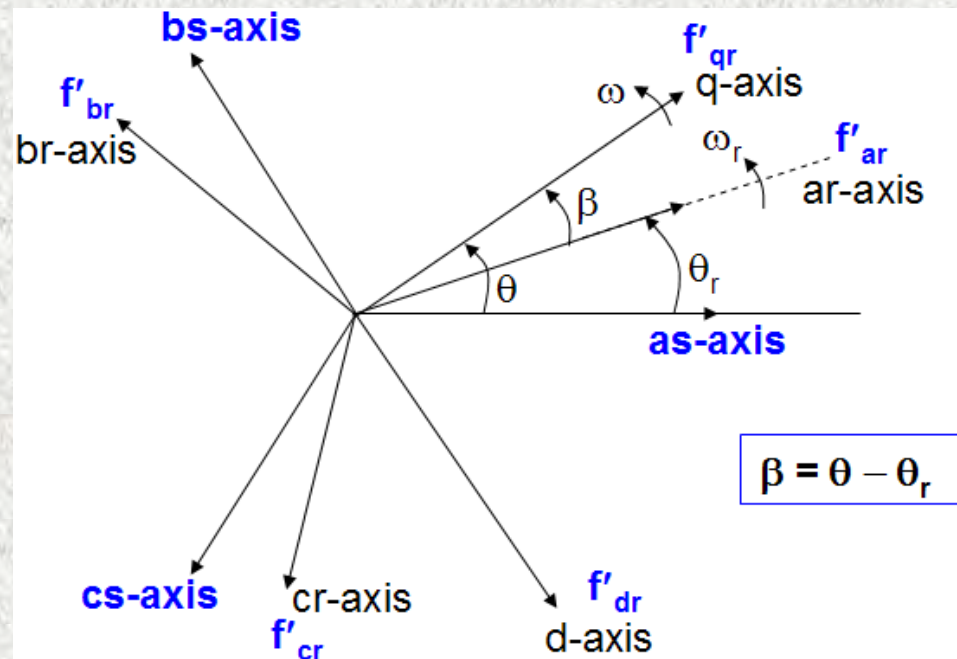
$$(f'_{abcr})^T = \begin{bmatrix} f'_{ar} & f'_{br} & f'_{cr} \end{bmatrix}$$

$$\mathbf{K}_r = \frac{2}{3} \begin{bmatrix} \cos \beta & \cos(\beta - \frac{2\pi}{3}) & \cos(\beta + \frac{2\pi}{3}) \\ \sin \beta & \sin(\beta - \frac{2\pi}{3}) & \sin(\beta + \frac{2\pi}{3}) \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix},$$

Transformation of Rotor Windings to the Arbitrary Reference Frame

where, $\beta = \theta - \theta_r$

$$\theta_r = \int_0^t \omega_r(t) dt + \theta_r(0)$$



$$(\mathbf{K}_r)^{-1} = \begin{bmatrix} \cos \beta & \sin \beta & 1 \\ \cos(\beta - \frac{2\pi}{3}) & \sin(\beta - \frac{2\pi}{3}) & 1 \\ \cos(\beta + \frac{2\pi}{3}) & \sin(\beta + \frac{2\pi}{3}) & 1 \end{bmatrix}$$

“r” subscript indicates the variable, parameters and transformation associated with rotating circuits.

Voltage Equations in Arbitrary Reference Frame Variables

- For two-pole, 3-phase symmetrical induction,

$$\bar{V}_{abcs} = \bar{r}_s i_{abcs} + p \lambda_{abcs}$$

$$V'_{abcr} = r'_r i'_{abcr} + p \lambda'_{abcr}$$

$$\lambda_{abcs} = (\bar{L}_s) i_{abcs} + (L'_{sr}) i'_{abcr}$$

$$\lambda'_{abcr} = (\bar{L}'_{sr})^T i_{abcs} + (L'_r) i'_{abcr}$$

$$\bar{V}_{abcs} = \mathbf{K}_s \bar{V}_{qd0s}, \quad i_{abcs} = \mathbf{K}_s i_{qd0s}$$

$$V'_{abcr} = \mathbf{K}_r \bar{V}'_{qd0r}, \quad i'_{abcr} = \mathbf{K}_r i'_{qd0s}$$

Voltage Equations in Arbitrary Reference Frame Variables

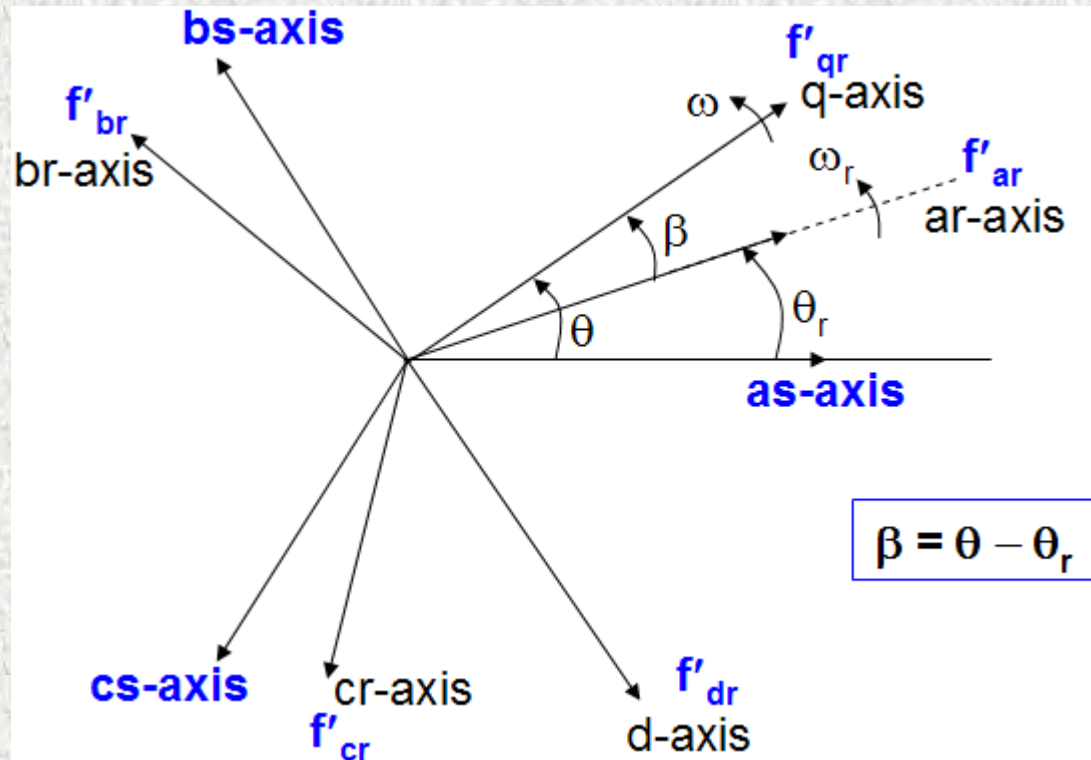


Fig.1 Axis of 2-pole, 3-phase symmetrical induction.

Voltage Equations in Arbitrary Reference Frame Variables

- Using the above transformation equations, we can transform the voltage equations to an arbitrary reference frame rotating at speed of ω .

$$V_{qd0s} = r_s i_{qd0s} + \omega \lambda_{qds} + p \lambda_{qd0s}$$

$$V'_{qd0r} = r'_r i_{qd0r} + (\omega - \omega_r) \lambda'_{qdr} + p \lambda'_{qd0r}$$

where, $(\lambda_{qds})^T = [\lambda_{ds} \quad -\lambda_{qs} \quad 0]$, $(\lambda'_{qdr})^T = [\lambda'_{dr} \quad -\lambda'_{qr} \quad 0]$

- Flux linkage equations in abc reference frame can be transformed to qd axes using K_s and K_r transformation matrices.

Voltage Equations in Arbitrary Reference Frame Variables

$$\begin{bmatrix} \lambda_{qd0s} \\ \lambda'_{qd0r} \end{bmatrix} = \begin{bmatrix} \mathbf{K}_s \mathbf{L}_s (\mathbf{K}_s)^{-1} & \mathbf{K}_s \mathbf{L}'_{sr} (\mathbf{K}_r)^{-1} \\ \mathbf{K}_r \mathbf{L}'_{sr} (\mathbf{K}_s)^{-1} & \mathbf{K}_r \mathbf{L}'_r (\mathbf{K}_r)^{-1} \end{bmatrix} \begin{bmatrix} i_{qd0s} \\ i'_{qd0r} \end{bmatrix}$$

where,

$$\mathbf{K}_s \mathbf{L}_s (\mathbf{K}_s)^{-1} = \begin{bmatrix} L_{ls} + M & 0 & 0 \\ 0 & L_{ls} + M & 0 \\ 0 & 0 & L_{ls} + M \end{bmatrix}, \quad M = \frac{3}{2} L_{ms}$$

$$\mathbf{K}_r \mathbf{L}'_r (\mathbf{K}_r)^{-1} = \begin{bmatrix} L'_{lr} + M & 0 & 0 \\ 0 & L'_{lr} + M & 0 \\ 0 & 0 & L'_{lr} + M \end{bmatrix}, \quad M = \frac{3}{2} L_{ms}$$

Voltage Equations in Arbitrary Reference Frame Variables

$$\mathbf{K}_s \mathbf{L}'_{sr} (\mathbf{K}_r)^{-1} = \mathbf{K}_r (\mathbf{L}'_{sr})^T (\mathbf{K}_s)^{-1} = \begin{bmatrix} M & 0 & 0 \\ 0 & M & 0 \\ 0 & 0 & M \end{bmatrix}$$

- Voltage equations in expanded form:

$$V_{qs} = r_s i_{qs} + \omega \lambda_{ds} + p \lambda_{qs} \quad V'_{qr} = r'_r i'_{qr} + (\omega - \omega_r) \lambda'_{dr} + p \lambda'_{qr}$$

$$V_{ds} = r_s i_{ds} - \omega \lambda_{qs} + p \lambda_{ds}, \quad V'_{dr} = r'_r i'_{dr} - (\omega - \omega_r) \lambda'_{qr} + p \lambda'_{dr}$$

$$V_{0s} = r_s i_{0s} + p \lambda_{0s} \quad V'_{0r} = r'_r i'_{0r} + p \lambda'_{0r}$$

- Flux linkage equations are

$$\lambda_{qs} = L_{ls} i_{qs} + M (i_{qs} + i'_{qr}) \quad \lambda'_{qr} = L'_{lr} i'_{qr} + M (i_{qs} + i'_{qr})$$

$$\lambda_{ds} = L_{ls} i_{ds} + M (i_{ds} + i'_{dr}) \quad \lambda'_{dr} = L'_{lr} i'_{dr} + M (i_{ds} + i'_{dr})$$

$$\lambda_{0s} = L_{ls} i_{0s} \quad \lambda'_{0r} = L'_{lr} i'_{0r}$$

Voltage Equations in Arbitrary Reference Frame Variables

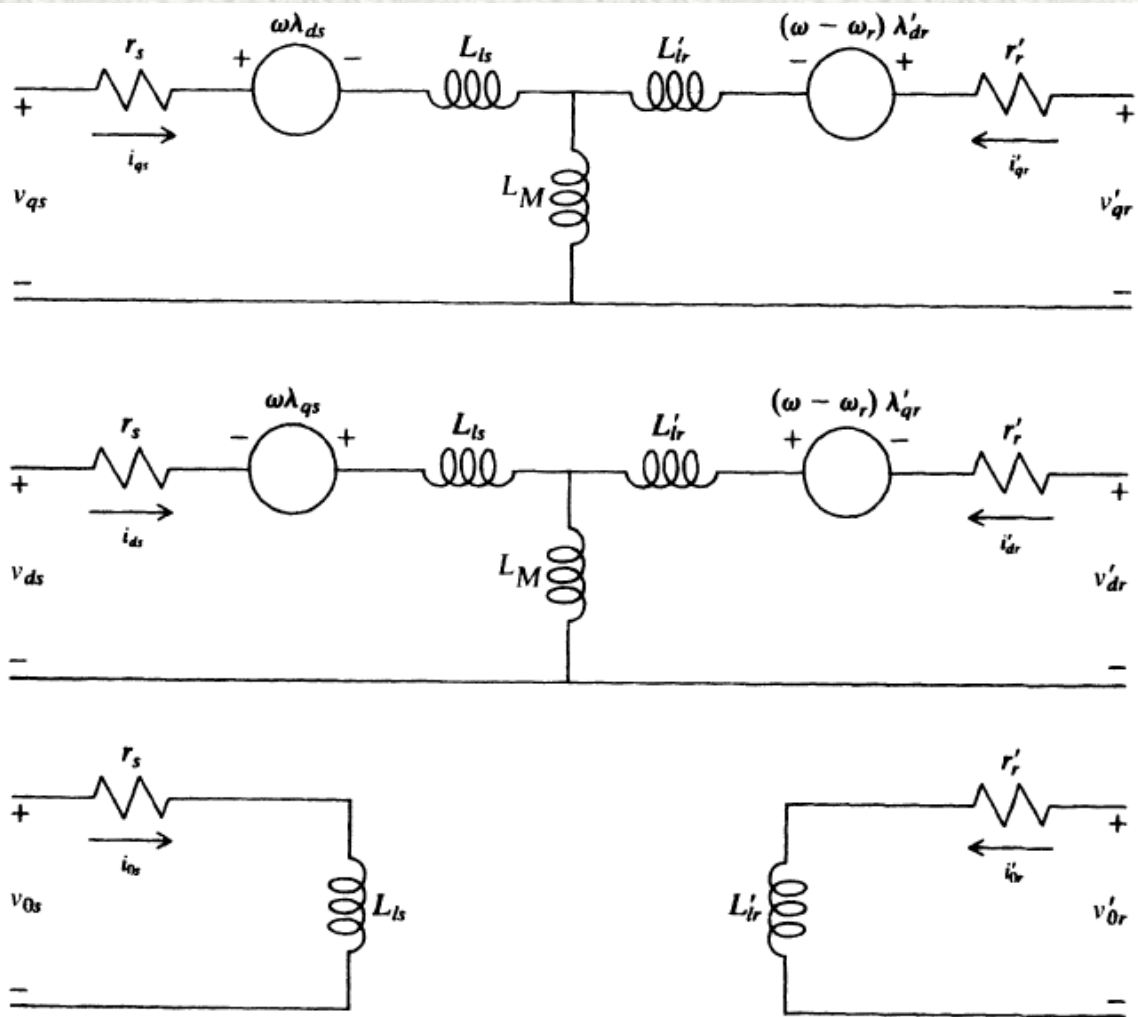


Figure 4.5-1 Arbitrary reference-frame equivalent circuits for a 3-phase, symmetrical induction machine.

Voltage Equations in Arbitrary Reference Frame Variables

■ Since machine and power system parameters are nearly always given in ohms or percent or per unit of a base impedance, it is convenient to express the voltage and flux linkage equations in terms of reactances rather than inductances. Let:

$$\varphi = \lambda \omega_b$$

■ Then

$$V_{qs} = r_s i_{qs} + \frac{\omega}{\omega_b} \varphi_{ds} + p \varphi_{qs}$$

$$V'_{qr} = r'_r i'_{qr} + \frac{(\omega - \omega_r)}{\omega_b} \varphi'_{dr} + \frac{p}{\omega_b} \varphi'_{qr}$$

$$V_{ds} = r_s i_{ds} - \frac{\omega}{\omega_b} \varphi_{qs} + \frac{p}{\omega_b} \varphi_{ds},$$

$$V'_{dr} = r'_r i'_{dr} - \frac{(\omega - \omega_r)}{\omega_b} \varphi'_{qr} + \frac{p}{\omega_b} \varphi'_{dr}$$

$$V_{0s} = r_s i_{0s} + \frac{p}{\omega_b} \varphi_{0s}$$

$$V'_{0r} = r'_r i'_{0r} + \frac{p}{\omega_b} \varphi'_{0r}$$

Voltage Equations in Arbitrary Reference Frame Variables

- Where flux linkages become flux linkages per second with the units of volts.

$$\begin{aligned} \varphi_{qs} &= X_{ls} i_{qs} + X_m (i_{qs} + i'_{qr}) & \varphi'_{qr} &= X'_{lr} i'_{qr} + X_m (i_{qs} + i'_{qr}) \\ \varphi_{ds} &= X_{ls} i_{ds} + X_m (i_{ds} + i'_{dr}), & \varphi'_{dr} &= X'_{lr} i'_{dr} + X_m (i_{ds} + i'_{dr}) \\ \varphi_{0s} &= X_{ls} i_{0s} & \varphi'_{0r} &= X'_{lr} i'_{0r} \end{aligned}$$

$$\begin{bmatrix} v_{qs} \\ v_{ds} \\ v_{0s} \\ v'_{qr} \\ v'_{dr} \\ v'_{0r} \end{bmatrix} = \begin{bmatrix} r_s + \frac{p}{\omega_b} X_{ss} & \frac{\omega}{\omega_b} X_{ss} & 0 & \frac{p}{\omega_b} X_M & \frac{\omega}{\omega_b} X_M & 0 \\ -\frac{\omega}{\omega_b} X_{ss} & r_s + \frac{p}{\omega_b} X_{ss} & 0 & -\frac{p}{\omega_b} X_M & \frac{p}{\omega_b} X_M & 0 \\ 0 & 0 & r_s + \frac{p}{\omega_b} X_{ls} & 0 & 0 & 0 \\ \frac{p}{\omega_b} X_M & \left(\frac{\omega - \omega_r}{\omega_b}\right) X_M & 0 & r'_r + \frac{p}{\omega_b} X'_{rr} & \left(\frac{\omega - \omega_r}{\omega_b}\right) X'_{rr} & 0 \\ -\left(\frac{\omega - \omega_r}{\omega_b}\right) X_M & \frac{p}{\omega_b} X_M & 0 & -\left(\frac{\omega - \omega_r}{\omega_b}\right) X'_{rr} & r'_r + \frac{p}{\omega_b} X'_{rr} & 0 \\ 0 & 0 & 0 & 0 & 0 & r'_r + \frac{p}{\omega_b} X'_{lr} \end{bmatrix} \begin{bmatrix} i_{qs} \\ i_{ds} \\ i_{0s} \\ i'_{qr} \\ i'_{dr} \\ i'_{0r} \end{bmatrix}$$

$$X_{ss} = X_{ls} + X_M$$

$$X'_{rr} = X'_{lr} + X_M$$

$$\begin{bmatrix} \psi_{qs} \\ \psi_{ds} \\ \psi_{0s} \\ \psi'_{qr} \\ \psi'_{dr} \\ \psi'_{0r} \end{bmatrix} = \begin{bmatrix} X_{ss} & 0 & 0 & X_M & 0 & 0 \\ 0 & X_{ss} & 0 & 0 & X_M & 0 \\ 0 & 0 & X_{ls} & 0 & 0 & 0 \\ X_M & 0 & 0 & X'_{rr} & 0 & 0 \\ 0 & X_M & 0 & 0 & X'_{rr} & 0 \\ 0 & 0 & 0 & 0 & 0 & X'_{lr} \end{bmatrix} \begin{bmatrix} i_{qs} \\ i_{ds} \\ i_{0s} \\ i'_{qr} \\ i'_{dr} \\ i'_{0r} \end{bmatrix}$$

$$\begin{bmatrix} i_{qs} \\ i_{ds} \\ i_{0s} \\ i'_{qr} \\ i'_{dr} \\ i'_{0r} \end{bmatrix} = \frac{1}{D} \begin{bmatrix} X'_{rr} & 0 & 0 & -X_M & 0 & 0 \\ 0 & X'_{rr} & 0 & 0 & -X_M & 0 \\ 0 & 0 & \frac{D}{X_{ls}} & 0 & 0 & 0 \\ -X_M & 0 & 0 & X_{ss} & 0 & 0 \\ 0 & -X_M & 0 & 0 & X_{ss} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{D}{X'_{lr}} \end{bmatrix} \begin{bmatrix} \psi_{qs} \\ \psi_{ds} \\ \psi_{0s} \\ \psi'_{qr} \\ \psi'_{dr} \\ \psi'_{0r} \end{bmatrix}$$

where

$$D = X_{ss}X'_{rr} - X_M^2$$

Torque Equation in Arbitrary Reference Frame Variables

- Electromagnetic torque in terms of arbitrary reference frame variables may be obtained by substituting the equations of transformation in

$$\begin{aligned}
 T_e &= \frac{P}{2} (i_{abcs})^T \frac{\partial}{\partial \theta_r} (L'_{sr}) i'_{abcr} \\
 &= \frac{P}{2} [(\mathbf{K}_s)^{-1} i_{qd0s}]^T \frac{\partial}{\partial \theta_r} (L'_{sr}) (\mathbf{K}_r)^{-1} i'_{qd0r}
 \end{aligned}$$

- After some work, we will have the following:

$$T_e = \left(\frac{3}{2} \right) \left(\frac{P}{2} \right) M (i_{qs} i'_{dr} - i_{ds} i'_{qr})$$

Torque Equation in Arbitrary Reference Frame Variables

- Where, T_e is positive for motor action. Other expressions for the electromagnetic torque of an induction machine are

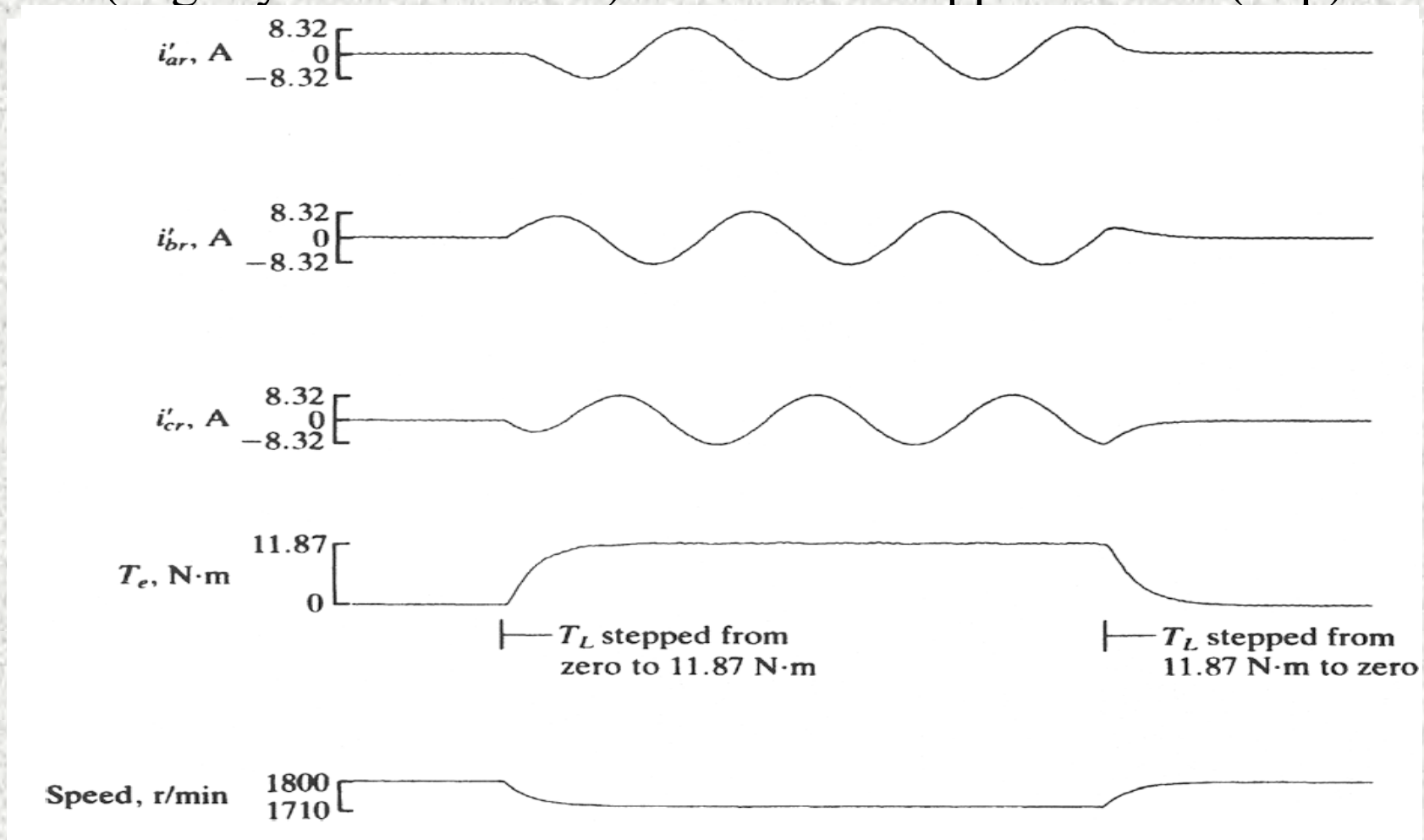
$$T_e = \left(\frac{3}{2}\right)\left(\frac{P}{2}\right)(\lambda'_{qr}i'_{dr} - \lambda'_{dr}i'_{qr})$$

$$T_{em} = \left(\frac{3}{2}\right)\left(\frac{P}{2}\right)(\lambda_{ds}i_{qs} - \lambda_{qs}i_{ds})$$

$$T_e = \left(\frac{3}{2}\right)\left(\frac{P}{2}\right)\left(\frac{1}{\omega_b}\right)(\phi'_{qr}i'_{dr} - \phi'_{dr}i'_{qr})$$

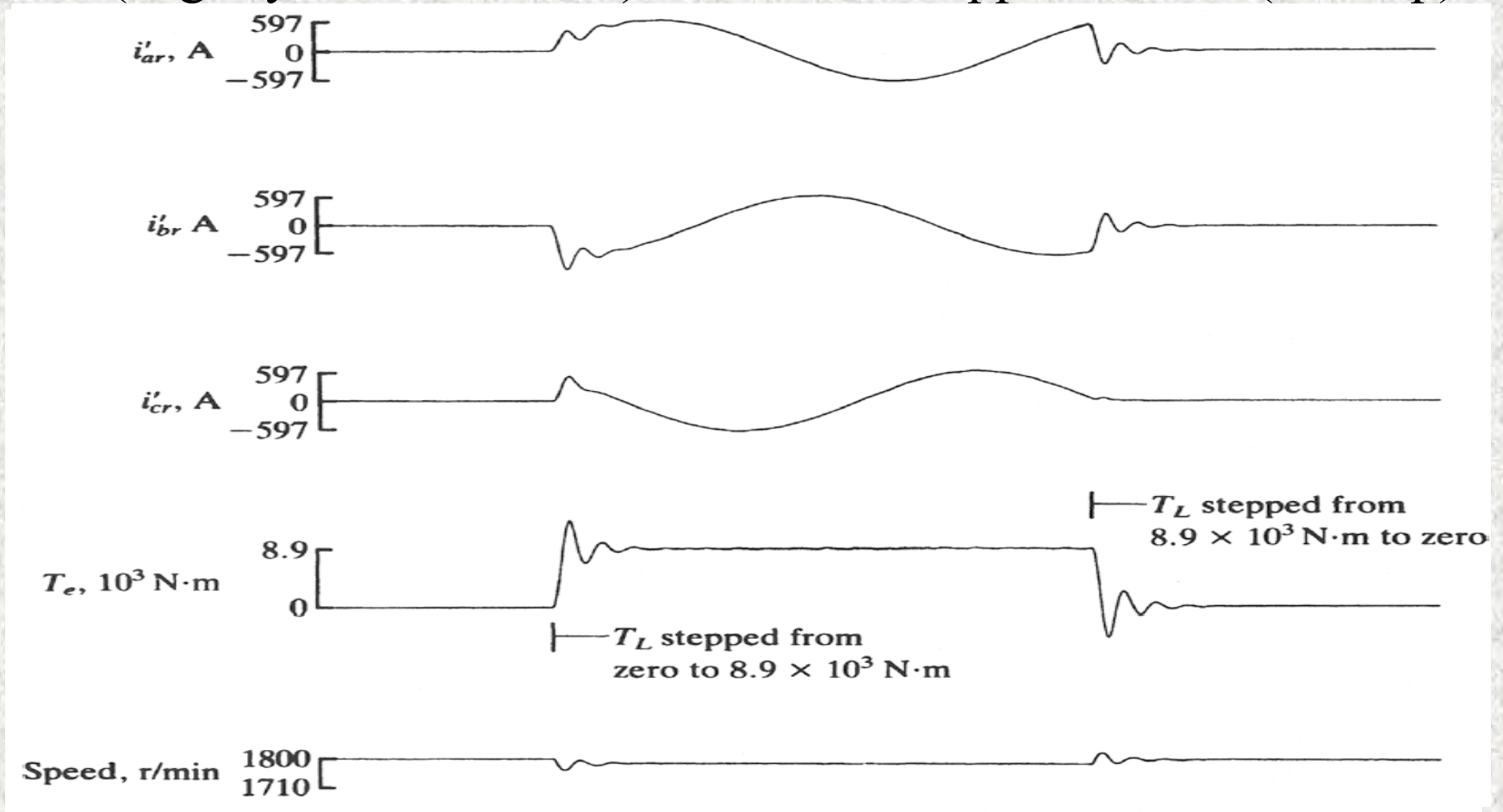
DYNAMIC PERFORMANCE DURING SUDDEN CHANGES IN LOAD TORQUE

- The load torque is first stepped from zero to base torque (slightly less than rated) and then is stepped to zero (3hp)



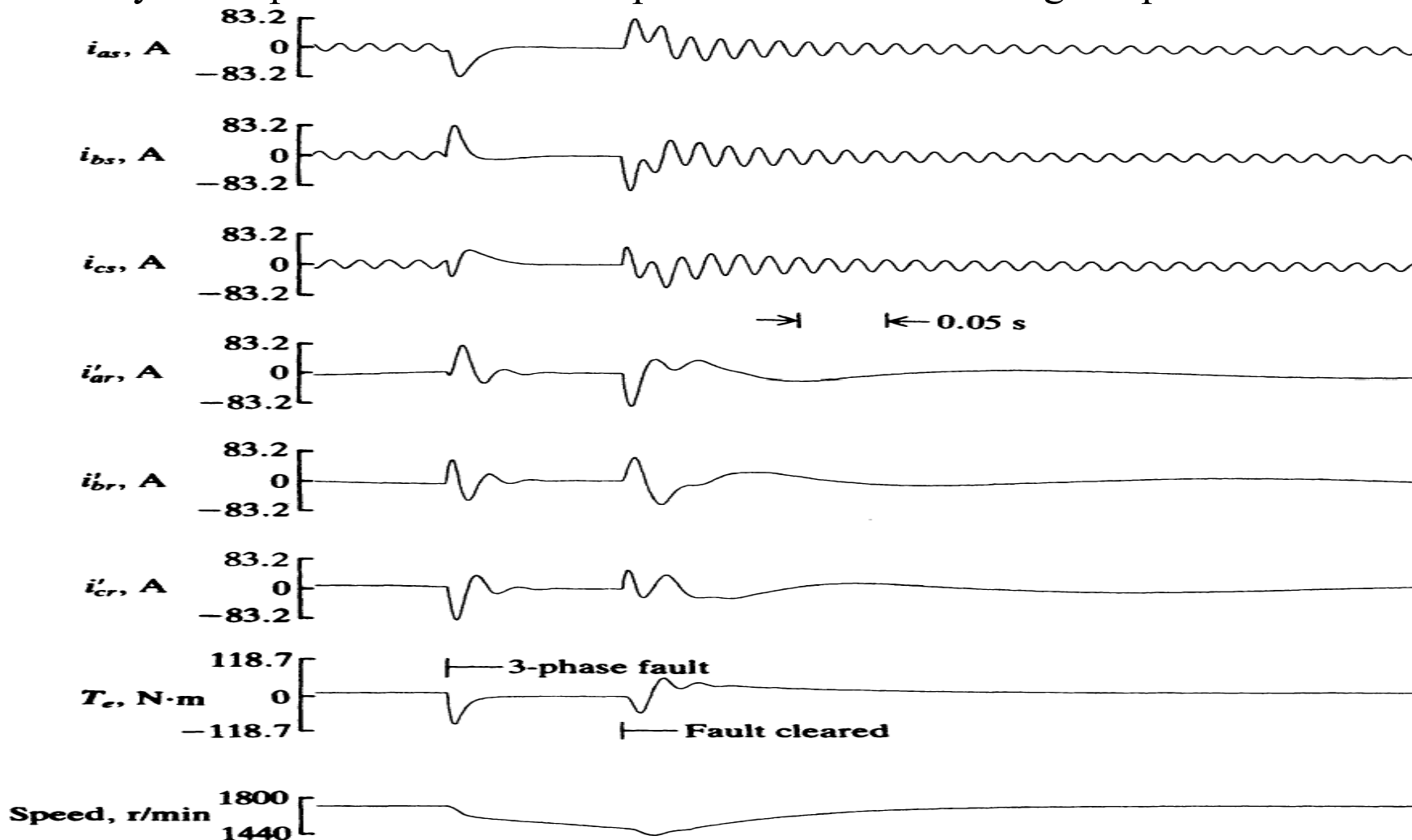
DYNAMIC PERFORMANCE DURING SUDDEN CHANGES IN LOAD TORQUE

- The load torque is first stepped from zero to base torque (slightly less than rated) and then is stepped to zero (2250hp)

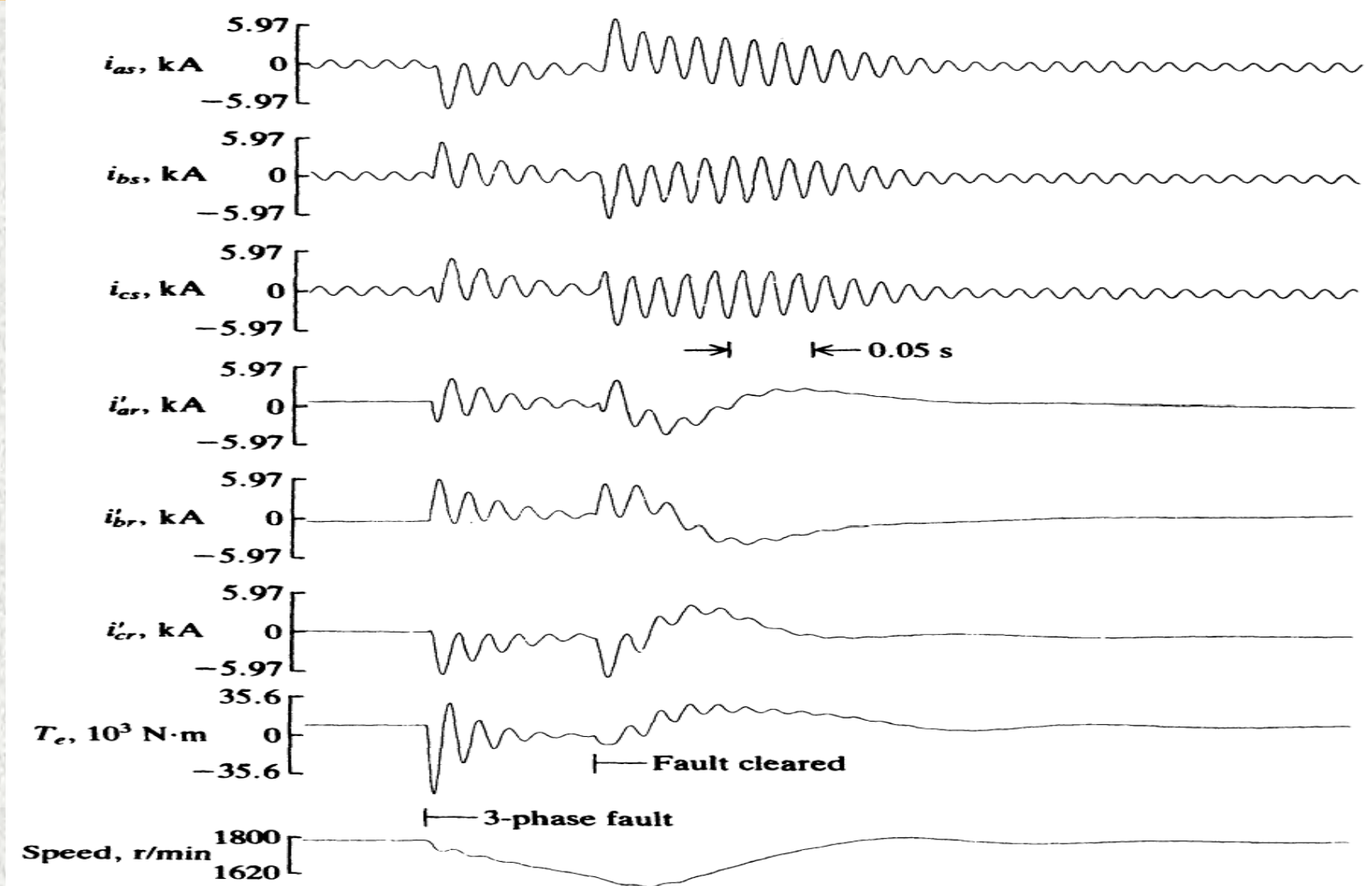


DYNAMIC PERFORMANCE DURING A 3-PHASE FAULT AT THE MACHINE TERMINALS

Dynamic performance of a 3-hp induction motor during a 3-phase fault

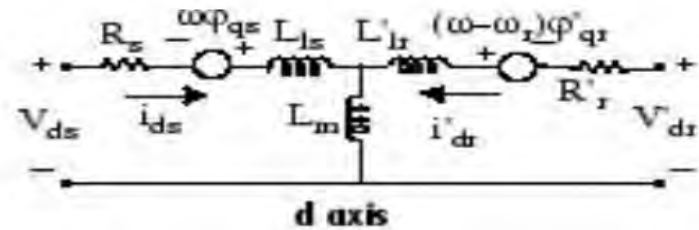
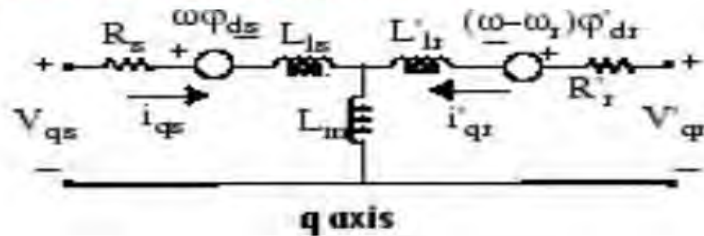


DYNAMIC PERFORMANCE DURING A 3-PHASE FAULT AT THE MACHINE TERMINALS



COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

Electrical System



$$V_{qs} = R_s i_{qs} + \frac{d}{dt} \varphi_{qs} + \omega \varphi_{ds}$$

$$V_{ds} = R_s i_{ds} + \frac{d}{dt} \varphi_{ds} - \omega \varphi_{qs}$$

$$V'_{qr} = R'_r i'_{qr} + \frac{d}{dt} \varphi'_{qr} + (\omega - \omega_r) \varphi'_{dr}$$

$$V'_{dr} = R'_r i'_{dr} + \frac{d}{dt} \varphi'_{dr} - (\omega - \omega_r) \varphi'_{qr}$$

$$T_e = 1.5 p (\varphi_{ds} i_{qs} - \varphi_{qs} i_{ds})$$

$$\varphi_{qs} = L_s i_{qs} + L_m i'_{qr}$$

$$\varphi_{ds} = L_s i_{ds} + L_m i'_{dr}$$

$$\varphi'_{qr} = L'_r i'_{qr} + L_m i_{qs}$$

$$\varphi'_{dr} = L'_r i'_{dr} + L_m i_{ds}$$

$$L_s = L_{ls} + L_m$$

$$L'_r = L'_{lr} + L_m$$

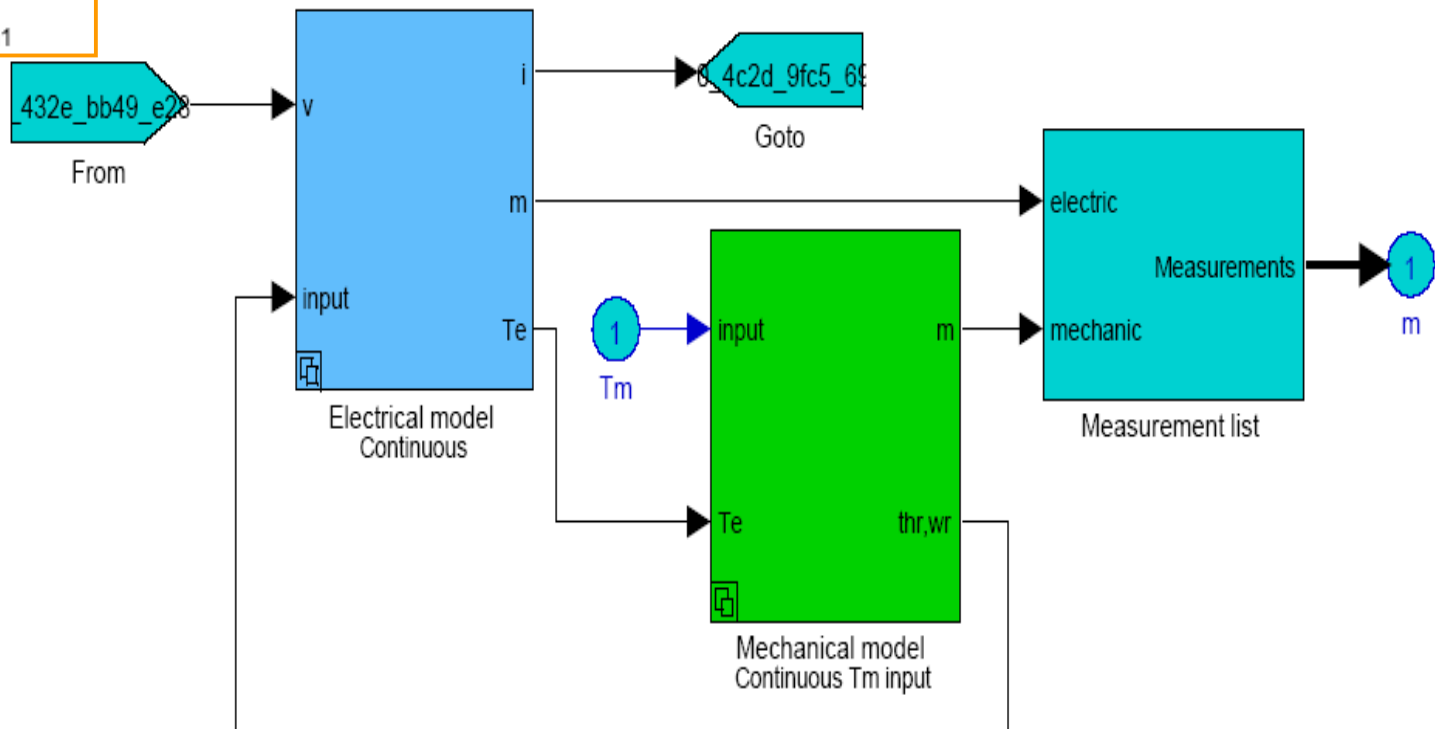
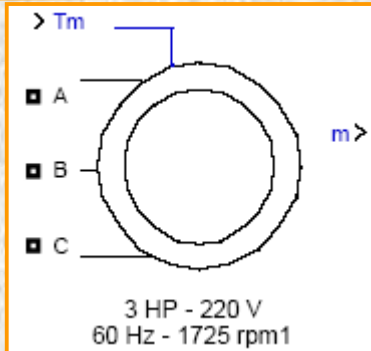
where

Mechanical System

$$\frac{d}{dt} \omega_m = \frac{1}{2H} (T_e - F \omega_m - T_m)$$

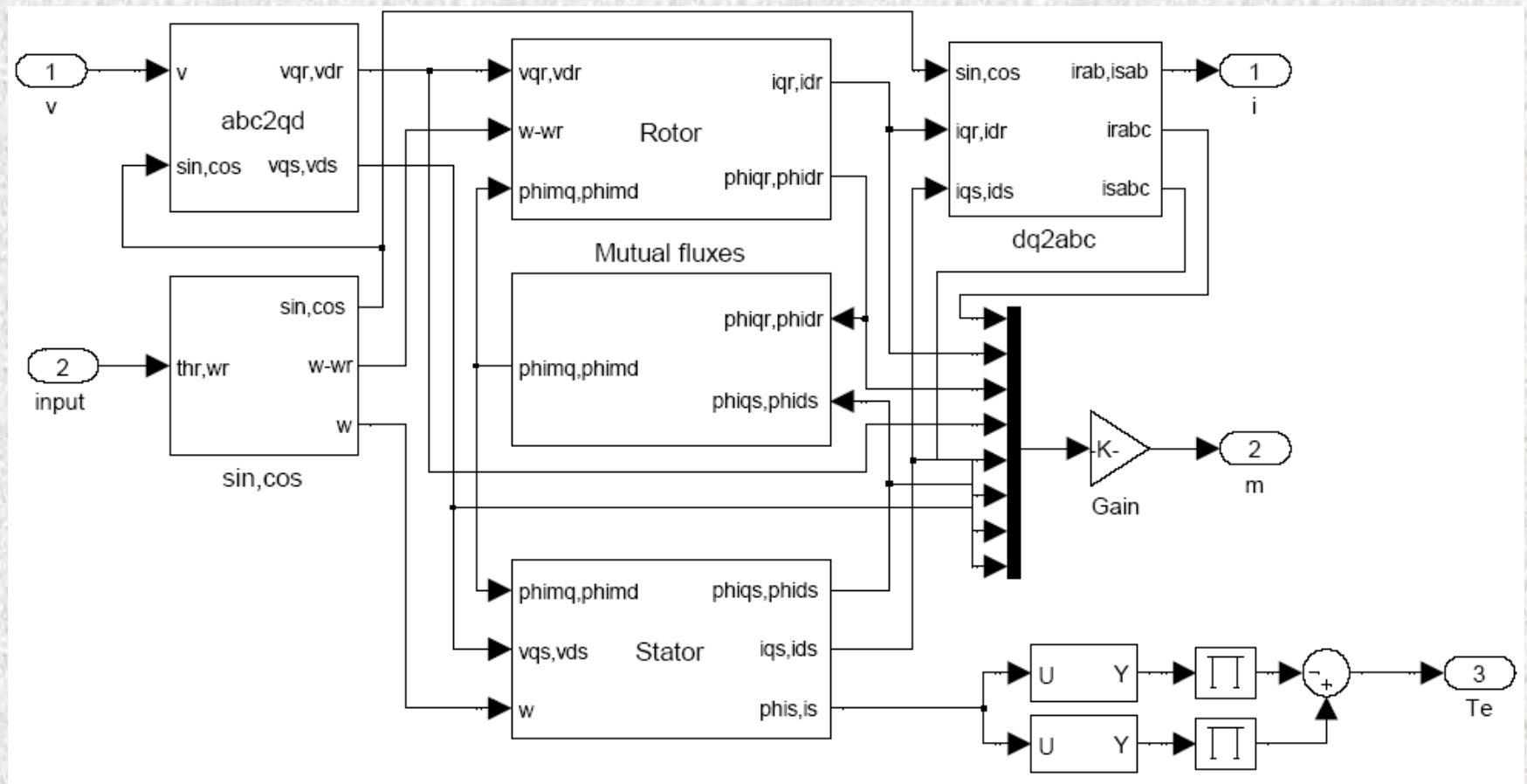
$$\frac{d}{dt} \theta_m = \omega_m$$

COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME



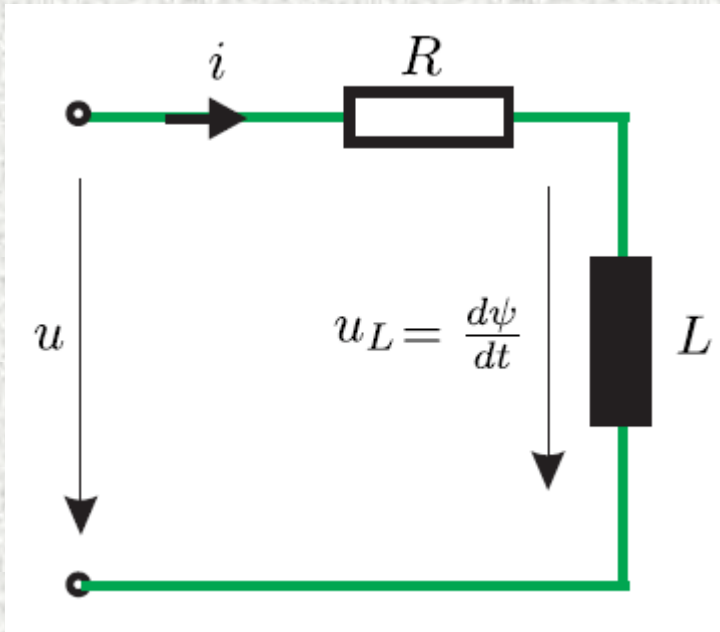
COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

Electrical model



COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

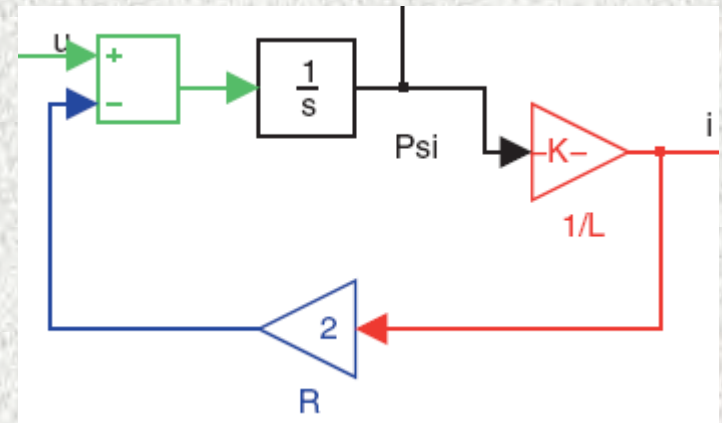
RL Circuit Simulink model



$$u = iR + \frac{d\psi}{dt}$$

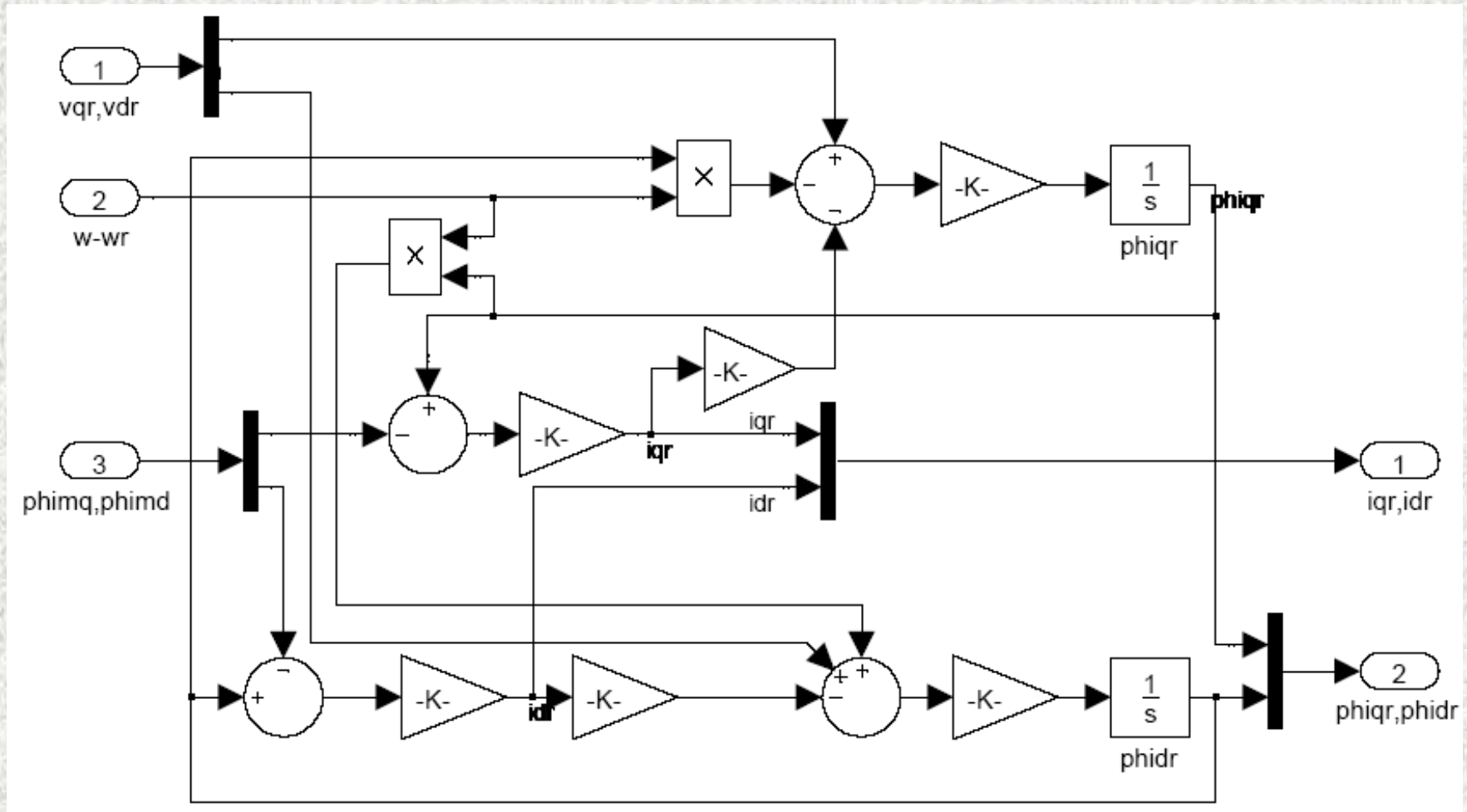
$$\psi = Li$$

$$u = \frac{R}{L}\psi + \frac{d\psi}{dt}$$



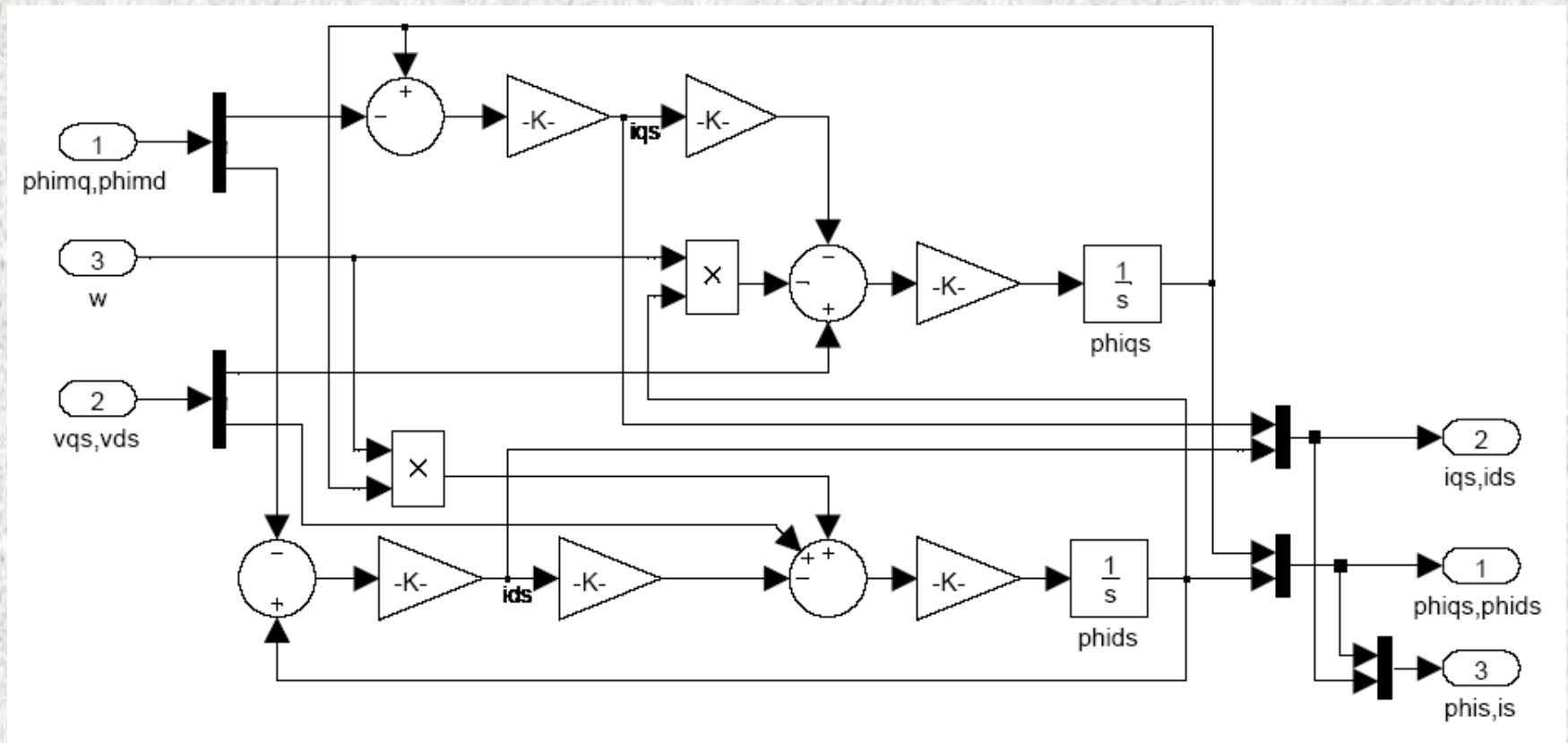
COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

Rotor model



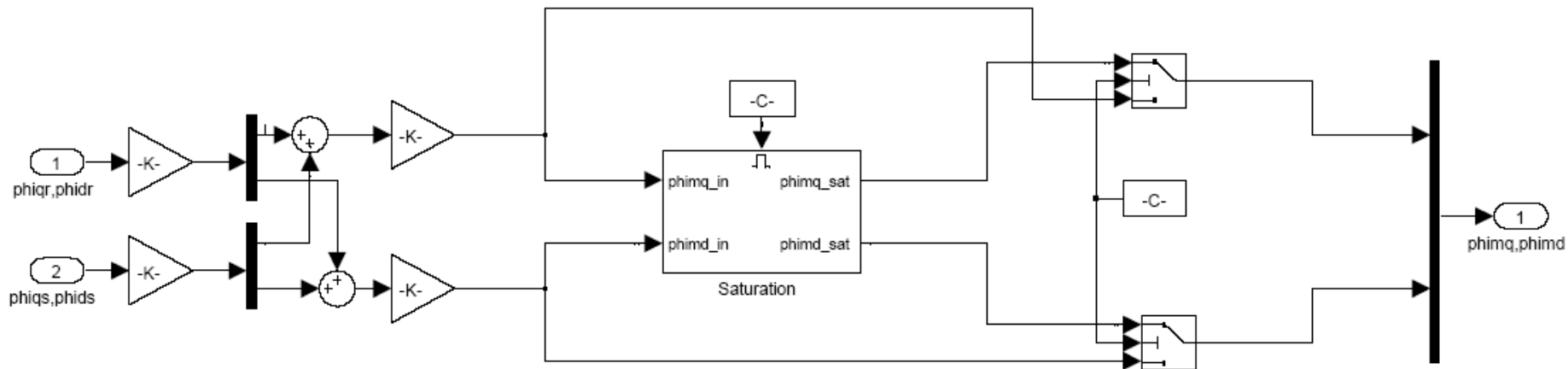
COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

Stator model



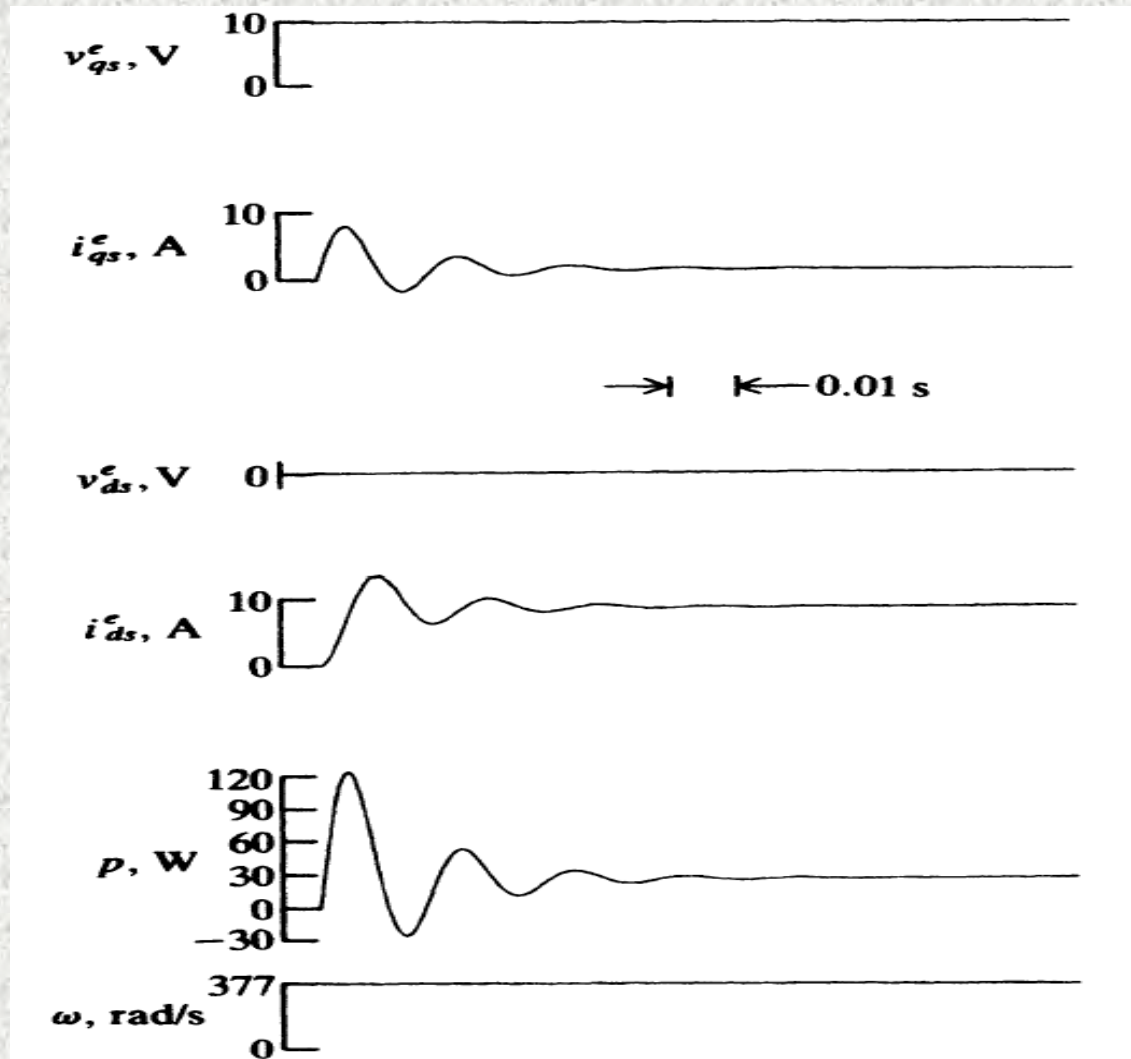
COMPUTER SIMULATION IN THE ARBITRARY REFERENCE FRAME

Mutual Fluxes model



Variables Observed From Several Frames of Reference

■ In Synchronous Reference Frame



Variables Observed From Several Frames of Reference

■ In Strange Reference Frame

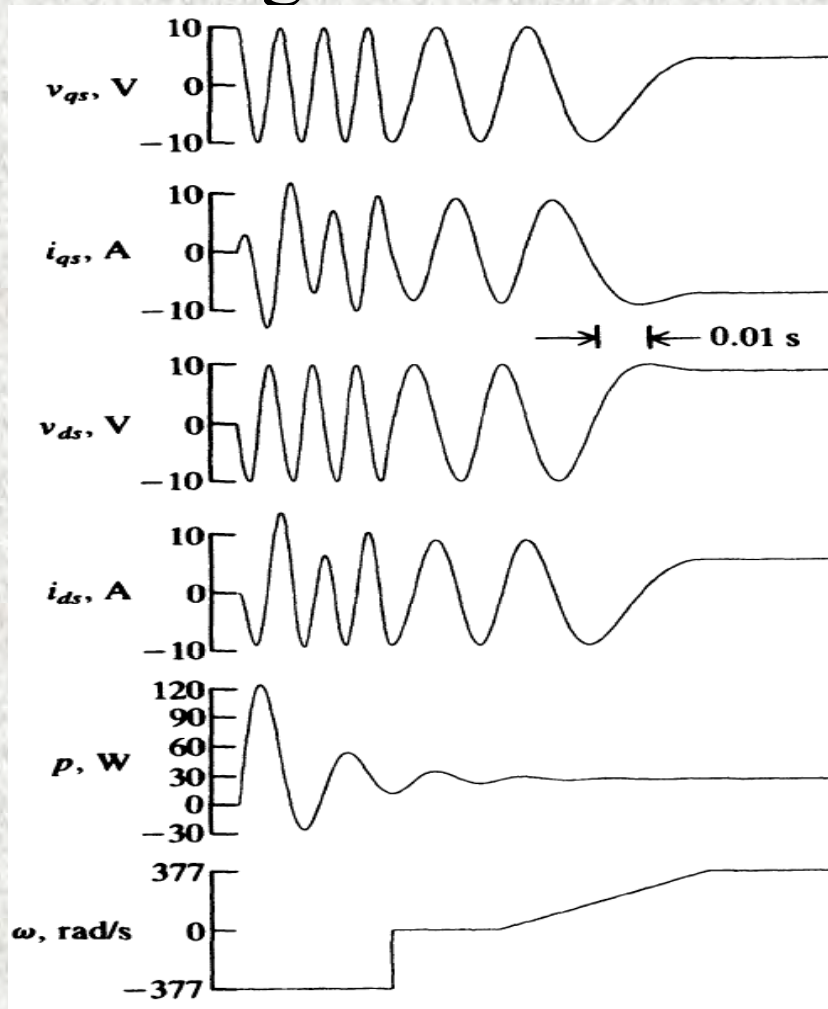


Figure 3.10-3 Variables of a stationary 3-phase system. First with $\omega = -\omega_e$, then ω is stepped to zero followed by a ramp change in reference frame speed to $\omega = \omega_e$.